

Software Engineering Department  
Braude College

Capstone Project Phase A – 61998

**Mapping Changes in Large Networks**

**25-1-R-13**

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<https://github.com/yossishemtov/Mapping-Change-in-Large-Networks-final-project.git>

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# **Abstract**

This project proposes a new framework for analyzing and mapping structural changes in large-scale dynamic networks, using journal citation networks as a case study. It focuses on identifying patterns, trends, and transformations over time, addressing the limitations of traditional statistical models in distinguishing meaningful trends from noise in complex networks.

The approach combines advanced algorithms GraphSAGE++, FastGCN, and HDBSCAN to process large-scale data efficiently. It generates dynamic node embeddings, clusters nodes with similar characteristics, and detects significant structural changes. Citation networks are analyzed across sequential periods, with HDBSCAN clustering identifying dense regions and labeling outliers as noise. Key transitions, such as cluster splits, mergers, and emerging groups, are visualized using alluvial diagrams to reveal trends and shifts in research focus.

By integrating these methods, the framework overcomes the challenges of scalability, noise filtering, and trend detection, providing insights into structural transformations applicable to fields like transportation, biology, and finance.

# **1. Introduction**

Analyzing large networks is essential for understanding complex systems. Various tools are designed to highlight prominent features and simplify these structures. These tools effectively reveal the static organization of networks but often fall short in tracking how these structures change over time. Understanding such changes is critical in systems like global air traffic, social contact networks during disease outbreaks, financial markets, or gene regulatory networks in health and disease [9].

Mapping network changes requires distinguishing meaningful trends from random noise, which traditional statistical models often fail to do. Clustering techniques provide a more effective alternative, allowing the analysis of systems with diverse and interacting elements.

Real-world networks, such as global air traffic or citation networks, are singular and cannot be replicated. This uniqueness makes common sampling approaches ineffective. Instead, advanced techniques like parametric bootstrap resampling are used to assess the significance of network clusters. These methods preserve the network's integrity by resampling link weights while maintaining the unique characteristics of nodes.

To visualize structural and functional changes, alluvial diagrams provide an intuitive way to track and summarize network evolution. This approach has broad applications, such as studying changes in transportation, finance, and scientific disciplines, enabling a deeper understanding of the dynamics driving network transformations over time.

# **2. Related Work and Problem Definition**

## **2.1 Problem Definition**

Large networks are widely used to represent complex systems across various domains, such as social interactions, scientific collaborations, or biological processes. These networks consist of nodes (vertices) and edges, capturing relationships and interactions within the system. As these networks evolve, understanding and mapping their structural changes is critical to uncovering patterns, trends, and transformations.

The problem focuses on identifying and analyzing changes within large dynamic networks. The input consists of a sequence of large networks, each representing interactions or relationships over specific periods. These networks serve as snapshots of the system at various times, enabling an analysis of how they evolve.

The primary purpose is to cluster these networks using advanced methods designed for large-scale data. This clustering process identifies meaningful structural components within the networks, setting the foundation for tracking changes over time. By applying appropriate methodologies, the objective is to detect and visualize the trend of changes, highlighting how clusters or network structures transform.

However, this task presents significant challenges:

1. **Scalability**: Large networks often contain millions of nodes and edges, making computations intensive and requiring efficient algorithms.
2. **Noise Filtering**: Real-world networks include random movements and noise that can Hide meaningful trends. Distinguishing between actual structural changes and random shifts is a critical challenge.
3. **Detecting Significant Trends**: Identifying patterns and transformations that are statistically and structurally significant is complex, especially when dealing with large datasets over multiple periods.

This study focuses on replacing the existing solution algorithm with a new, more advanced approach that leverages modern technology. The goal is to enhance insights into the dynamic nature of large-scale networks and better track their evolution over time.

## **2.2 Related works**

Mapping changes in large networks is critical to understanding the evolution of complex systems, and several methods are proposed to address this challenge. Rosvall and Bergstrom (2010) introduced a method using bootstrap resampling and significance clustering to distinguish between meaningful structural changes and noise in citation networks, visualizing these changes with alluvial diagrams [9]. Girvan and Newman (2002) proposed a modularity-based method to detect network community structures, showing that removing edges with high betweenness centrality reveals changing cluster structures over time [4]. Palla et al. (2005) presented the Clique Percolation Method (CPM) to detect overlapping communities and track the persistence of cliques across time intervals [8]. Giumarra and Amaral (2005) developed a method to identify functional modules in biological networks and studied how these modules change roles over time to adapt to different conditions [5]. Blondel et al. (2008) proposed the Louvain method for fast community detection and explored how community structures change by iteratively optimizing modularity in evolving networks [2]. Annaud and Guillaume (2010) explored methods for detecting communities in dynamic networks by comparing snapshots over time and introduced temporal smoothing to capture transitions between network states better [1]. The suggested articles explore methods for detecting changes in large networks, focusing on tracking evolving groups and visualizing structural changes over time in various domains such as social and biological networks. These approaches aim to analyze dynamic networks efficiently and effectively.

### **2.2.1. TRNN-GCN Algorithm: Limitations**

The Transitional Recurrent Graph Convolutional Network (TRNNGCN) combines Recurrent Neural Networks (RNNs) and Graph Convolutional Networks (GCNs) for dynamic clustering [10]. This algorithm introduces a decay rate to adjust the weight of historical data in clustering decisions, which allows the model to:

1. **Adapt to Changing Clusters:** Nodes with higher turnover rates can decay faster to account for recent changes, while stable nodes retain their historical weights.
2. **Learn Decay Dynamically**: Using an RNN layer, the algorithm learns optimal decay rates based on the graph’s evolution, applying this decay before clustering with GCN layers.
3. **Preserve Meaning and Clarity:** The decay rates clearly indicate how much importance is given to historical versus recent data for each cluster.

### **2.2.2. Key Features of the TRNNGCN Approach**

* **Dynamic Stochastic Block Model**: The algorithm models dynamic graphs using a stochastic block model to estimate probabilities of connections within and between clusters over time.
* **Decay Rates**: Introduces a decay rate matrix that adjusts edges' weights based on their relevance over time, improving clustering accuracy.
* **Iterative Learning**: TRNNGCN refines its clustering decisions over time steps by updating cluster memberships and decay rates.
* **Visualization**: Decay rates make the process meaningful, showing how each cluster evolves and adapts.

The Transitional Recurrent Graph Convolutional Network (TRNNGCN) algorithm clusters evolving graphs by adapting to network changes over time. It works well with dynamic graphs but uses too much memory and processing power for exceptionally large networks, making it hard to handle fast-growing data.

To address these challenges, two advanced methods are applied to handle the clustering of large data networks.

### **2.2.3. Selected Clustering Algorithms for Large-Scale Networks**

1. **FASTGCN**:
   1. FASTGCN (Fast Graph Convolutional Network) is a scalable variation of GCN designed to handle large datasets efficiently by lowering the heavy computational load that comes with processing the entire network at once. This method uses a sampling technique. Instead of aggregating data from every node's full neighborhood, it selects a smaller sample to represent the neighborhood. This approach saves both memory and processing time, making the algorithm much more efficient.
   2. This method allows for real-time graph data processing while maintaining high accuracy in clustering results, making it ideal for analyzing large networks.
2. **GraphSAGE++**:
   1. GraphSAGE++ builds on the original GraphSAGE (Graph Sample and Aggregate) algorithm by enhancing the aggregation process to handle even larger datasets. It introduces optimizations for distributed processing and parallelism, enabling faster computation on large-scale networks.
   2. Unlike traditional GCNs, GraphSAGE++ learns node embeddings by sampling and aggregating features from a fixed-size neighborhood, making it scalable and efficient for large dynamic graphs.

In this capstone, we discuss both FASTGCN and GraphSAGE++ in detail, exploring their architectures, advantages, and applicability to dynamic network clustering. Combining these two methods aims to create a comprehensive framework for analyzing and mapping changes in large-scale networks over time. This dual-clustering strategy addresses the limitations of TRNNGCN while providing the scalability needed for real-world applications.

**3. Mathematical Background**

## **3.1 GraphSAGE++**

Before delving into the GraphSAGE++ clustering algorithm, it is important first to outline the foundational methods upon which it is built. These methods offer the necessary background and context for understanding the algorithm's operation.

### **3.1.1. Aggregator Functions and Key Concepts and Definitions**

The aggregator function is a crucial component of GraphSAGE, responsible for combining the features of a node's neighbors into a single representation. For GraphSAGE, the aggregator must satisfy symmetry (i.e., the output should be invariant to the order of neighbors) because the neighborhood of a node does not have an inherent ordering. Below are the three main types of aggregators used:

**Mean Aggregator**

The mean aggregator is one of the simplest and most used aggregation methods. It computes the element-wise mean of the feature vectors of the neighboring nodes.

Mathematically:

* : Aggregated features for node v at layer K.
* N(v): Set of neighbors of node v.
* : Representation of neighbor from the previous layer.

This method is computationally efficient and performs well for tasks where the aggregated features can be represented as a linear combination.

**LSTM Aggregator**

The LSTM aggregator leverages a Long Short-Term Memory (LSTM) network to aggregate the neighbors' features. LSTMs can capture more complex relationships between features by processing them sequentially.

Steps:

1. The neighbors' feature vectors are treated as a sequence.
2. A random permutation of the neighbors is used since LSTMs are not inherently symmetric.
3. The LSTM processes this sequence and outputs an aggregated representation .

Mathematically, the LSTM updates are:

**Pooling Aggregator**

The pooling aggregator is a two-step process:

* Each neighbor's feature vector is independently passed through a fully connected neural network:

where:

* + W and b are trainable parameters.
  + is a non-linear activation function (e.g., ReLU).
* An element-wise max pooling operation aggregates the transformed neighbor features:

,

where:

* + Maxis applied elementwise across all the feature vectors.

The pooling aggregator captures the most prominent features across the neighborhood, making it highly capable and suitable for capturing diverse characteristics.

: Fixed Number of Neighbors

represents the fixed number of neighbors sampled at each layer k for every node. Sampling ensures that the computation remains efficient, even in exceptionally large graphs where nodes might have hundreds or thousands of neighbors.

For example:

* If a node v has 100 neighbors, and ,GraphSAGE will randomly select 10 neighbors of v during the aggregation step.
* This fixed sampling size controls the computational complexity, ensuring that the number of operations is proportional to the depth K and the sample size at each layer.

Wpool and bpool : Weights and Biases for Pooling

These are trainable parameters used in the pooling aggregator:

* Wpool: Weight matrix applied to the neighbor's feature vector .
* pool: Bias vector added after applying the weight matrix.

In the pooling aggregator:

1. Each neighbor's feature vector is transformed using a fully connected layer:

* + Wpool: Captures the relationship between input features.
  + bpool: Adds a shift to the transformation.

2. The transformed feature vectors are aggregated using element-wise max pooling:

.

This step ensures that the model captures the most expressive features from the neighborhood.

### **3.1.3 GraphSAGE++ Algorithm steps**

GraphSAGE++ objective is to generate low-dimensional embeddings for nodes in a graph by sampling and aggregating features from a node's local neighborhood. This approach is particularly useful for clustering large networks, as it captures both local and global structural information [7].

1. **Graph :** 
   1. V: Set of nodes.
   2. E: Set of edges connecting nodes.
2. **Node Features :**
   1. Each node v has an associated feature vector .
3. **Hyperparameters:**
   1. Depth K**:** Number of layers (or hops).
   2. Aggregator functions for .
   3. Weight matrices for each layer.
   4. Non-linearity (e.g., ReLU).

**Algorithm’s steps**

**1. Initialization:** Set the initial representation of each node to its input features:

**2. Neighborhood Sampling:** Define the neighborhood for each node **v.** In large graphs, uniformly sample a fixed-size subset of neighbors at each layer kto ensure computational efficiency.

**3. Iterative Aggregation and Update:** For k= 1 to K (where K is the depth of the algorithm):

* **Step 1 - Neighbor Aggregation:** Aggregate features of neighbors using the k-th aggregator function:

Examples:

* + - **Mean Aggregator:**
    - **Pooling Aggregator:**
* **Step 2 - Update Node Representation** Combine the node's current representation with the aggregated neighbor features, then apply a dense layer with non-linearity:

Here, **CONCAT** denotes the concatenation of vectors.

**4. Normalization (Optional)** Normalize node embeddings after each layer:

**5. Output** After K iterations, the final embeddings for each node are:

**Output**

The algorithm outputs for all nodes , where:

* : Low-dimensional embedding of node v, capturing structural and feature-based information from its K-hop neighborhood.
* These embeddings can be used for downstream tasks such as clustering, node classification, or link prediction.

**Computational Complexity**

GraphSAGE reduces the memory and computational footprint by:

Sampling neighbors instead of using the full neighborhood.

Fixing per-batch complexity at , where is the sample size at depth k.

**Summary of the GraphSAGE Pipeline**

1. **Input:** Graph, node features, depth K, and hyperparameters.
2. **Neighbor Aggregation:** Aggregates information from sampled neighbors using symmetric functions.
3. **Feature Propagation:** Combines node features with aggregated neighborhood features across K layers.
4. **Output:** Node embeddings representing the graph's local and global structure.

## **3.2 FastGCN algorithm**

### **3.2.1 Definitions and Core Concepts**

Before delving into the phases of FastGCN, it is necessary to clarify the mathematical and conceptual elements that the algorithm relies on. These elements are crucial for understanding its phases and overall functioning.

**Graph Convolution:**

* Traditional graph convolution in GCN updates the node embeddings by aggregating information from neighbors.
* The mathematical formulation is:

where:

* + : Node embeddings at the layer .
  + A: Normalized adjacency matrix of the graph.
  + : trainable weight matrix for layer
  + : Non-linear activation function (e.g., ReLU).

**Monte Carlo Sampling:**

* FastGCN views graph convolutions as integral transforms:

where is a probability distribution over nodes . This formulation enables sampling nodes to estimate the integral using Monte Carlo methods.

**Importance Sampling:**

* To reduce the difference, nodes are sampled using a probability distribution designed to minimize the variance of the embedding updates. The optimal It is created to focus more on important nodes by considering their role and connections within the network.

**Embedding Generation:**

* Node embeddings are iteratively refined through layers. For sampled nodes, the embeddings are updated as:

where is the sampled set of neighbors.

### **3.2.2 STEPS of the FastGCN Algorithm**

1. **Input:**
   * A graph
   * with:
     + : Nodes,
     + : Edges,
   * Node feature matrix

(where n is the number of nodes and is the feature dimension).

* + Normalized adjacency matrix
  + Number of layers
  + Sampling distribution .
  + Trainable weight matrices for each for each layer .

1. **Node Sampling:**
   * Instead of aggregating all neighbors, FastGCN samples a fixed number of nodes at each layer .
   * Sampling is performed using a probability distribution , where:
2. **Layer-wise Convolution:**
   * For each layer :
     + Nodes are sampled,
     + The embeddings are updated using the sampled neighbors:

.

1. **Variance Reduction:**
   * Importance sampling is employed to ensure that frequently sampled nodes contribute proportionally to their influence in the graph.
2. **Loss Calculation:**
   * The loss function **L** is defined over a subset of labeled nodes for semi-supervised learning. For classification:

Where predicted label distribution for node .

1. **Optimization:**
   * Stochastic Gradient Descent (SGD) is used to minimize the loss. Gradients are calculated only for sampled nodes at each layer.
2. **Output:**
   * The final embeddings are used for downstream tasks like node classification or clustering.

## **3.3 HDBSCAN cluster algorithm**

After generating node embeddings for the graph using algorithms such as GraphSAGE++ or FastGCN, the graph is clustered based on these embeddings using the HDBSCAN clustering algorithm [7].

### **3.3.1 Algorithm Steps**

**Step 1: Core Distance Calculation**

For each point :

* Define the core distance, , as the distance to its k-th nearest neighbor, where

.

* Mathematically:

**Step 2: Mutual Reachability Distance**

For any two points and , compute the mutual reachability distance:

* Ensures points are only connected if they both belong to dense regions.
* Introduces robustness to variations in density.

**Step 3: Build the Mutual Reachability Graph**

* Construct a graph where:
  + **Nodes**: Points in .
  + **Edges**: Weighted by .

**Step 4: Minimum Spanning Tree (MST)**

* Compute a minimum spanning tree (MST) on , which organizes points into a hierarchical structure:
  + **Nodes**: Same as .
  + **Edges**: A subset of that connects all nodes with minimal total weight.
  + Total weight:

**Step 5: Cluster Stability**

To evaluate the stability of clusters:

1. Define as the inverse of the mutual reachability distance:
   1. : Value of when the cluster forms.
   2. : Value of when the cluster dissolves.
2. Select clusters with the highest stability.

**Step 6: Extract Clusters**

* Extract clusters by analyzing the dendrogram and retaining only stable clusters.
* Points not belonging to any stable cluster are labeled as noise.

**Output**

1. **Cluster Labels:**
   1. Assign a cluster ID (e.g., 0, 1, 2, ...) to each point in .
   2. Noise points are labeled as -1.
2. **Cluster Properties:**
   1. Number of clusters, sizes, and representative points.

# **4. Project Overview**

## **4.1 Workflow**

The workflow involves analyzing large-scale networks over different periods to identify patterns, filter out irrelevant data, and track how the network structure changes over time. The process is divided into stages, with each step building on the results of the previous one.

Initially, citation network data are prepared by creating graphs representing different periods. Nodes represent entities like journals, and edges denote relationships such as citations. To improve data quality, self-citations are removed, resulting in cleaned graphs.

These graphs are then processed using embedding techniques like GraphSAGE++ or FastGCN, which generate compressed vector representations for each node. These embeddings capture structural and feature information, enabling clustering tasks.

The embeddings are input into the HDBSCAN algorithm, which identifies clusters without requiring a predefined number of clusters.

HDBSCAN assigns cluster labels based on dense regions in the feature space and Labels outliers as irrelevant data(noise), forming meaningful groupings such as research domains.

Using the Hungarian Method, transitions between clusters in consecutive time points are optimally matched based on shared nodes or feature similarity. This ensures precise identification of transitions such as splits, mergers, and new clusters.

Next, the clusters are analyzed to assign meaningful names based on node attributes, making computational results easier for humans to understand. This naming process makes the clusters more understandable and relevant.

Then, cluster evolution over time is visualized using alluvial diagrams, showing transitions such as splits, merges, and node movements between clusters. These visualizations highlight key trends, reveal emerging fields and focus shifts, and help distinguish significant changes from noise.

Finally, the alluvial diagrams and clustering results are reviewed to detect key trends, explain

changes, and generalize the findings to other network types.

## **4.2 Pseudocode**

**Input:** Dataset of citation networks for multiple time points: , where each graph consists of:

* N: Nodes (journals/articles).
* : Edges (citations between journals).
* : Weight of the edge from node a to node b (number of citations).
* : Node features matrix.

**Output:** Insights into network structural changes, visualized through alluvial diagrams, and interpreted meaningful trends.

**Step 1. Data Preparation**

Objective: Prepare and preprocess the input networks for analysis.

Input: Raw citation networks .

Output: Preprocessed graphs with normalized weights and feature vectors.

**a.** Collect citation network data for all time points .

**b.** Represent each graph as a directed, weighted graph:

* Nodes : Represent articles.
* Edges represent citation of article b in article a.

**d**. Integrate node feature vectors (e.g., word occurrence vectors or metadata features).

**Step 2. Embedding Generation**

Objective: Transform each node in the graph into an embedding vector.

Input: Preprocessed graphs with node features .

Output: Embedding vectors for each node in all graphs.

**a**. Input preprocessed graphs and node features into GraphSAGE++ or FastGCN.

**b**. For each graph , generate embedding vectors for all nodes :

* For GraphSAGE++, aggregate features from neighbors iteratively.

**OR**

* For FastGCN, sample nodes layer-wise to compute embeddings.

**c**. Output the embedding vectors for all nodes across all graphs.

**Step 3. Clustering**

Objective: Cluster nodes based on their embeddings to groups of similar nodes.

Input: Embedding vectors for nodes in

Output: Cluster labels for each node in all graphs

**a**. Input the embedding vectors into the HDBSCAN clustering algorithm.

**b**. Use HDBSCAN to assign cluster labels to nodes in each graph :

* Clusters represent groups of similar nodes.
* Noise points are labeled separately.

**c**. Output cluster labels for all nodes in .

**Step 4. Tracking Cluster Evolution**

Objective: Identify how clusters evolve.

Input: Cluster labels .

Output: Cluster transitions (mergers, splits, new clusters).

* **a**. Use the Hungarian method to match clusters in with clusters inbased on the size of shared nodes or feature similarity.

**b**. Identify transitions between clusters:

* Mergers: When two or more clusters in combine into one cluster in .
* Splits: When a cluster in divides into multiple clusters in .
* New Clusters: Clusters in that have no counterpart in .

**c**. Quantify transitions: Use the Hungarian method to compute the cost matrix based on shared nodes or similarity between clusters in and ​.

* Quantify the size and type of transitions (e.g., the percentage of shared nodes).

**d**. Output a map of cluster transitions across time points.

**Step 5. Constructing Alluvial Diagrams**

Objective: Visualize structural changes in the networks over time.

Input**:** Cluster transitions from the Hungarian method between graphs.

Output: Alluvial diagram illustrating cluster evolution.

**a**. Represent clusters for each time point as blocks in columns:

* The height of each block corresponds to the cluster size (number of nodes).

**b**. Use stream fields to connect blocks across time points:

* The width of each stream represents the transition size.
* Splits, mergers, and new clusters are highlighted.

**c**. Optimize visualization:

* Use smooth splines for streams.
* Exclude streams below a predefined size threshold to reduce clutter.

**d**. Output an alluvial diagram visualizing cluster evolution.

**Step 6. Insights and Interpretation**

Objective: Derive meaningful conclusions from the analysis.

Input: Alluvial diagrams and clustering results.

Output: Key trends, patterns, and their implications.

**a**. Analyze the alluvial diagrams and clustering results.

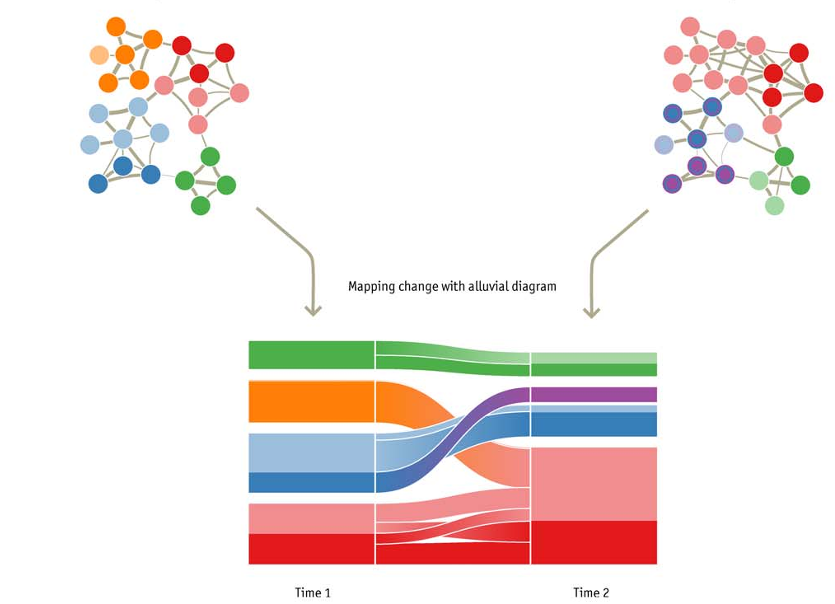
**b**. Identify key trends:

* Emerging fields or growing clusters.
* Declining clusters or merged topics.
* Stable clusters over time.

**c**. Explain observed changes:

* Link structural changes to external factors (e.g., research focus shifts, funding changes).

**d**. Generalize findings to other types of networks (e.g., social, economic).

Fig. 1. The Alluvial Diagram.   
This figure is taken from: [9]

# **5. Expected Achievements**

This research focuses on developing a new framework for mapping changes in large-scale networks using modern technologies and advanced algorithms. The process incorporates GraphSAGE++, FastGCN, and HDBSCAN methods to group nodes and efficiently identify meaningful structural changes over time. The goal is to provide a more accurate and scalable approach for analyzing large-scale networks, such as journal citation networks, allowing for a better understanding of key transformations and their impact across various domains.

# **6. Research / Engineering process**

## **6.1 The Process**

The research is divided into two main phases: Phase A and Phase B.

**Phase A:** Research and Learning

Phase A focuses on understanding core algorithms related to dynamic networks. The process began by studying "Mapping Changes in Large Networks" [9] to establish a foundation for tracking network changes over time. Following this, "Interpretable Clustering on Dynamic Graphs with Recurrent Graph Neural Networks" [10] was analyzed to explore a newer Cluster algorithm intended to replace the original method from [9].

Upon further evaluation, the Cluster algorithm from [10] was found to be insufficient for handling large citation networks. Therefore, the focus shifted to more advanced algorithms, including GraphSAGE++ [6], Fast GCN [3], and HDBSCAN [7], to improve clustering performance and scalability.

**Phase B:** Implementation

Phase B involved implementing the selected algorithms to perform clustering on large citation networks. The methods presented in [3], [6], and [7] were adapted to manage dynamic graphs efficiently.

Following the implementation of clustering and the generation of embedding vectors from large-scale networks, the overall algorithm will be developed based on the ideas presented in "Mapping Changes in Large Networks" [9], using methods such as GraphSAGE++, FastGCN, HDBSCAN, and Hungarian Method.

This approach provides a powerful and efficient tool for mapping and tracking changes in large citation networks over time, enabling the detection of significant structural transformations and emerging research trends.

This research aims to develop a new algorithm based on modern technologies to map and track structural changes in large citation networks over time. The proposed model consists of several steps to process, analyze, and visualize changes in large-scale networks over time.

The process begins by collecting citation networks from different periods, represented as directed, weighted graphs where nodes are articles and edges are citations. The networks are preprocessed by removing self-citations and normalizing edge weights.

Once the citation networks are prepared, they are fed into a graph embedding algorithm, either GraphSAGE++ or FastGCN, to transform each node into an embedding vector. These embedding vectors capture the structural and contextual information of each node in the network.

In the clustering phase, the embedding vectors generated from the previous step are input into the HDBSCAN algorithm. This step groups nodes with similar characteristics into clusters, where each cluster represents a group of related articles or research topics.

The next step is tracking how these clusters evolve over time by comparing cluster labels between consecutive graphs. To ensure precise tracking, the Hungarian Method is applied to optimally match clusters across time points based on shared nodes or feature similarity. This enhances the accuracy of identifying transitions, including mergers, splits, and the emergence of new clusters.

To visualize these changes, an alluvial diagram is constructed. The diagram represents clusters as blocks, with streamlines connecting them across different time points. The width of each streamline indicates the size of the transition, highlighting key events such as cluster splits, mergers, and the emergence of new clusters.

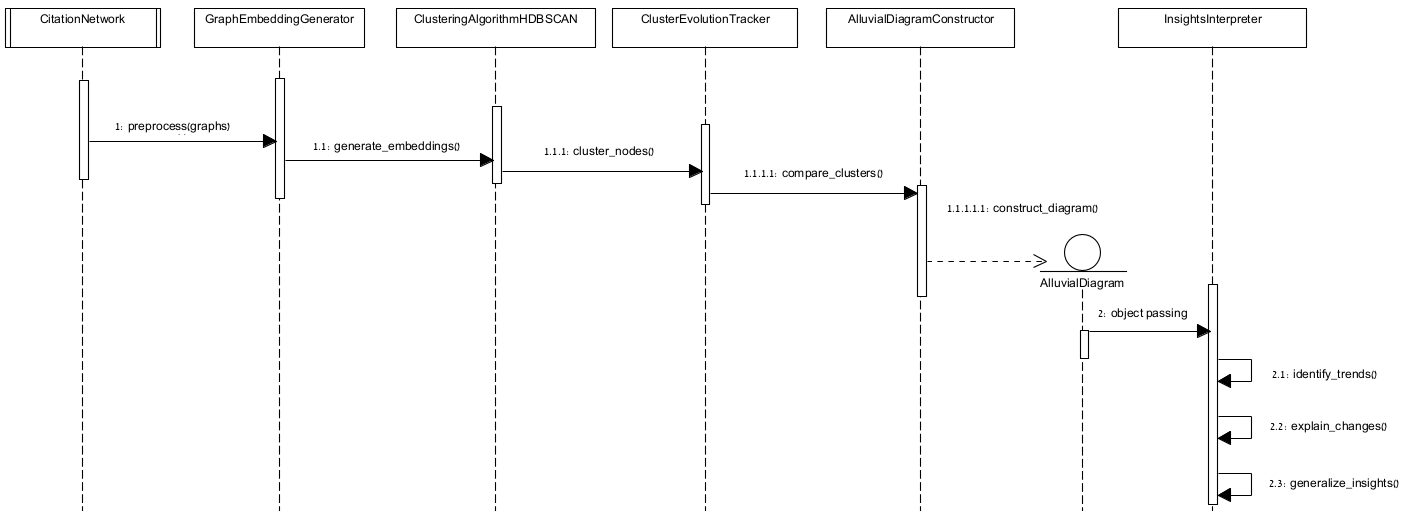
Finally, insights are derived from the clustering results and alluvial diagrams. Key trends, such as emerging research areas, declining topics, and stable domains, are identified.

### **6.2 Diagrams**

A diagram of a network

Description automatically generated*Class diagram*

*Sequence Diagram*

**

# **7. Evaluation and Testing Plan**

In part B of the research, we will focus on implementing the advanced algorithms FastGCN, GraphSAGE++, and HDBSCAN to enhance the clustering process in large citation networks. Additionally, we will implement the complete main process described in the "Mapping Changes in Large Networks" algorithm [9], which is designed to track significant structural changes in dynamic networks over time. This main algorithm processes large-scale citation networks by detecting evolving clusters, identifying trends such as emerging research areas, and recognizing topic splits or mergers.

## **7.1 Evaluation**

After fully implementing the framework, we will evaluate its accuracy and correctness by running the same dataset through our and existing reference implementations. The evaluation will focus on comparing the accuracy of the results produced by both implementations, ensuring that the proposed approach achieves equivalent precision in detecting clusters, emerging research areas, and structural changes in citation networks. By validating the consistency of the output, the objective is to confirm that the implementation correctly replicates the expected results while

optimizing computational performance**.**

## **7.2 Testing plan**

|  |  |  |  |
| --- | --- | --- | --- |
| **Index** | **Expected Result** | **Test Description** | **Component** |
| **1** | The graph preprocessing test ensures the graph is free of self-citations and has normalized weights | Test graph preprocessing | CitationNetwork |
| **2** | Nodes contain feature vectors | Test feature integration | CitationNetwork |
| **3** | Embedding vectors for all nodes in the graph | Generate embeddings using GraphSAGE++ | GraphEmbeddingGenerator |
| **4** | Embedding vectors for all nodes in the graph | Generate embeddings using FastGCN | GraphEmbeddingGenerator |
| **5** | Cluster labels assigned to each node | Perform clustering on embedding vectors | ClusteringAlgorithmHDBSCAN |
| **6** | Noise points labeled separately | Detect noise points | ClusteringAlgorithmHDBSCAN |
| **7** | Verify consistent clustering results across multiple runs | Cluster Stability Test | ClusteringAlgorithmHDBSCAN |
| **8** | Identify mergers, splits, and new clusters | Compare clusters between two consecutive graphs | ClusterEvolutionTracker |
| **9** | List of newly formed clusters | rack new clusters over time | ClusterEvolutionTracker |
| **10** | Alluvial diagram object created | Construct an alluvial diagram from cluster transitions | AlluvialDiagramConstructor |
| **11** | List of trends, including growing and declining clusters | Identify trends based on the alluvial diagram | InsightsInterpreter |
| **12** | Explanation of why certain clusters merged, split, or appeared | Explain changes in clusters | InsightsInterpreter |

# **8. Summary**

This research aims to develop a new process for analyzing large citation networks by implementing the core steps outlined in [9], using clustering algorithms such as GraphSAGE++, FastGCN, and HDBSCAN.

This approach involves building the entire workflow, including embedding generation, and clustering techniques, to improve the accuracy and efficiency of tracking significant structural changes in citation networks over time. The resulting system offers a more effective and innovative tool for detecting evolving research areas and trends.

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**Appendix A: AI Research Questions**

1. What are the principles of GraphSAGE++?
2. What are the principles of FastGCN?
3. What are embedding vectors?
4. How does HDBSCAN work?
5. What is the process of mapping structural changes in large data networks?
6. How is the evaluation conducted in this research?

**Appendix B: tools we used**

1. chat GPT

2. word